

How Google Searches Work

History of searching and the PageRank algorithm Martin Thoma, Benjamin Lipp | 7th of February, 2013

SPRACHENZENTRUM

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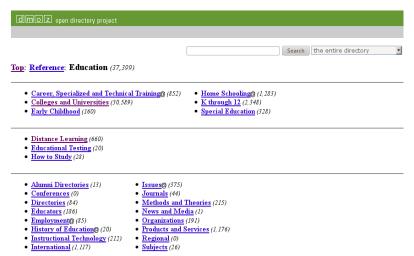
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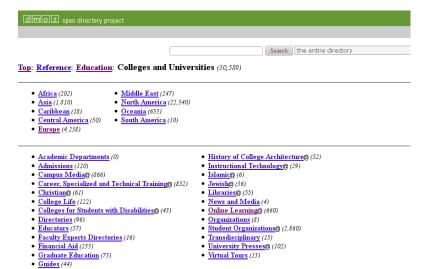


5,114,083 sites - 96,877 editors - over 1,014,849 categories









5/28



dmoz open directory project				
	about dmoz dmoz blog sugges			
	Search the entire directory			
<u>Top</u> : <u>Reference</u> : <u>Education</u> : <u>Colleges and Universities</u> : <u>Europe</u> (4,258)				
Academic Departments (0)				
Albania (8)	• Lithuania (9)			
• <u>Austria</u> (54)	• Luxembourg (1)			
• Belarus (11)	• Macedonia (19)			
• <u>Belgium</u> (24)	• <u>Malta</u> (14)			
 Bosnia and Herzegovina (8) 	• Moldova (1)			
 <u>Bulgaria</u> (30) 	• Montenegro (1)			
• Croatia (18)	• Netherlands (30)			
 Cyprus@ (1) 	• Norway (160)			
 Czech Republic (59) 	• Poland (175)			
 <u>Denmark</u> (11) 	• Portugal (6)			
 Estonia (23) 	• Romania (18)			
 Finland (23) 	• Russia (78)			
• France (19)	• <u>Serbia</u> (6)			
 Germany (121) 	• <u>Slovakia</u> (12)			
• <u>Greece</u> (22)	Slovenia (7)			
 Hungary (16) 	• Spain (20)			
• Iceland (4)	• <u>Sweden</u> (56)			



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<u>Top:</u> <u>Reference</u> : <u>Education</u> : <u>Colleges and Universities</u> : <u>Europe</u> : <u>Germany</u> (121)			
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See also:			
• Regional: Europe: Germany (3,998) • Regional: Europe: Germany: Education (11)			
This category in other languages:			
French (6) Gen	man (2,229)		



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<u>Top</u> : <u>Reference</u> : <u>Education</u> : <u>Colleges and Universities</u> : <u>Europe</u> : <u>Germany</u> : <u>Baden-Württemberg</u> (15)	
Hochschule Aslen - University of Applied Sciences (1) Hochschule Esslingen - University of Applied Sciences (1) Hochschule Furtwangen - University of Applied Sciences (0) Hochschule Heilbronn - Heilbronn University (1) Hochschule Konstanz - University of Applied Sciences (0) International University in Germany (1) Stuttgart Institute of Management and Technology (1) University of Freiburg (1) University of Stuttgart (1) University of Ulm (1)	ıeim
See also:	
• Regional: Europe: Germany: States: Baden-Württemberg: Education (1)	
This category in other languages:	
<u>German</u> (247)	

AOL - Ask - Bing - Gigablast - Google - Lycos - Yahoo - Yippy

• "Baden-Württemberg" search on:



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	about dmoz dmoz blog sugg
	Search the entire directory
<u>Fop</u> : <u>Reference</u> : <u>Education</u> : <u>Colleges and Universities</u> :	Europe: Germany: Baden-Württemberg: University of
ee also:	
Regional: Europe: Germany: States: Baden-Württember	org: Localities: Mannheim (2)
This category in other languages: German (7) • University of Mannheim - Offers undergraduate and graduate profinancial aid.	ograms; includes information on study and research at the university, directorie
• "University of Mannheim" search on:	AOL - Ask - Bing - Gigablast - Google - Lycos - Yahoo - Yippy
	Volunteer to edit this category.
Become an Editor Help build the largest human-edited directory of the web	



Search: uni mannhoim

Open Directory Categories (1-5 of 100)

- World: Français: Régional: Amérique: Etats-Unis: Etat et politique: Ambassades et consulats: Pays représentés (39)
- World: Deutsch: Wissen: Bibliotheken: Universitäts- und Hochschulbibliotheken: Deutschland (33)
- 3. World: Français: Régional: Amérique: Etats-Unis: Etat et politique: Ambassades et consulats: Représentations à l'étranger (24)
- 4. World: Nederlands: Maatschappij: Overheid: Europese Unie (22)
- World: Deutsch: Gesundheit: Krankenhäuser und Kliniken: Universitätskliniken: Deutschland (21)

more...

Open Directory Sites (1-20 of 15698)

- 1. amnesty international Hochschulgruppe Mannheim Die amnesty-Gruppe an der Uni Mannheim setzt sich unter anderem mit Petitionen, Appellbrief ein und stellt aktuelle Aktivitäten vor
 - -- http://www.amnesty-uni-mannheim.de/ World: Deutsch: Regional: Europa: Deutschland: Baden-Württemberg: Städte und Gemeinden: M. Mannheim: Gesellschaft (23)
- LHG Liberale Hochschulgruppe Mannheim Die liberale Studierenden an der Uni Mannheim stellen sich vor. -- http://www.uni-mannhaim.de/studorg/liberale/ World: Deutsch: Wissen: Bildung: Hochschulen: Europa: Deutschland: Baden-Württemberg: Universität Mannhaim ()
- Uni Mannheim Marktübersicht deutscher Anbieter für Online-Preisvergleiche. -- http://projekt.wifo.uni-mannheim.de/preisvergleich/ World: Deutsch: Zuhause: Verbraucherinformationen: Preisagenhuren: Ontine-Preisvergleiche ()
- 4. University of Mannheim Offers undergraduate and graduate programs; includes information on study and research at the university, directories of financial aid
 - -- http://www.uni-mannheim.de/ Reference: Education: Colleges and Universities: Europe: Germany: Baden-Württemberg: University of Mannheim ()

The Early Days: Web Crawlers





- crawls through the web using hyperlinks
- makes an index of the words contained in a page
- ranks pages for a search query according to number of occurences of keywords

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How can we use this massive amout of information?



- 625.3 million websites
- Wikipedia is one website and has several millions of pages
- ⇒ we need to rank websites!

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- X machines don't know what's good for humans
- humans create websites
- humans will only link to websites they like
- ⇒ hyperlinks are a quality indicator



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A Brilliant Idea







Sergey Brin

Larry Page



16/28

7th of February, 2013

- decisions of humans are complicated
- a lot of webpages get visited
- ⇒ modellize clicks on links as random behaviour
- links are important
 - links of page A get less important, if A has many links of page A get more important, if many link to A
- \Rightarrow if B has a link from A, the rank of B increases by $\frac{Rank(A)}{Links(A)}$

if A links to B then

$$Rank(B) += \frac{Rank(A)}{Links(A)}$$

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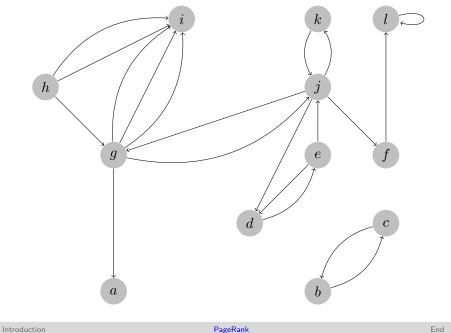
$$Rank(B) += \frac{Rank(A)}{Links(A)}$$

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What is PageRank?

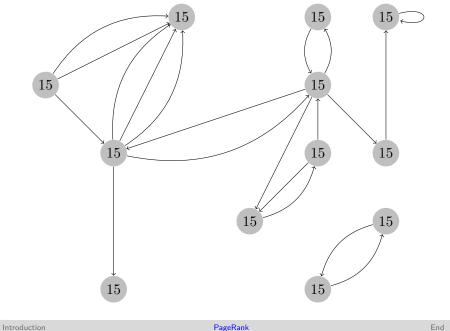


The PageRank algorithm calculates the probability of a randomly clicking user ending up on a given page.

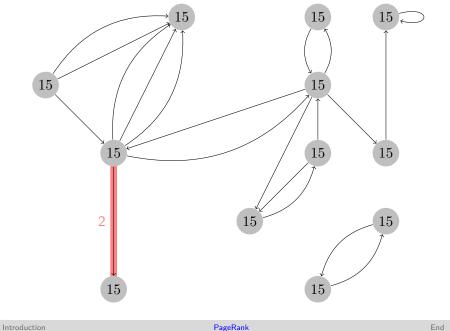


PageRank ○○○○○○●○○○ Martin Thoma, Benjamin Lipp - How Google Searches Work

End

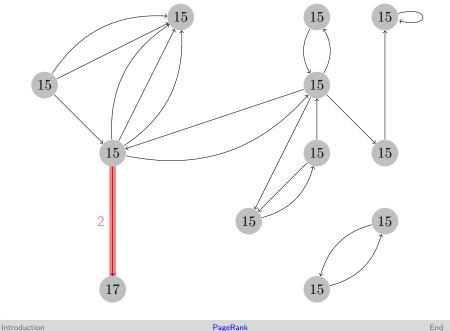


PageRank ○000000●00 Martin Thoma, Benjamin Lipp - How Google Searches Work



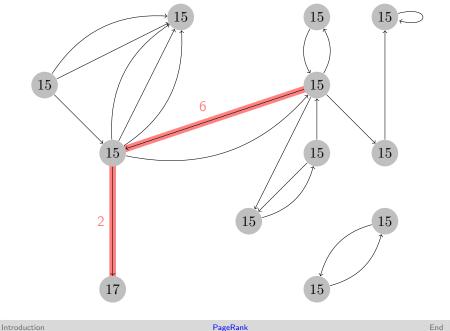
PageRank 00000000000

End 0000000 bruary, 2013 19/28



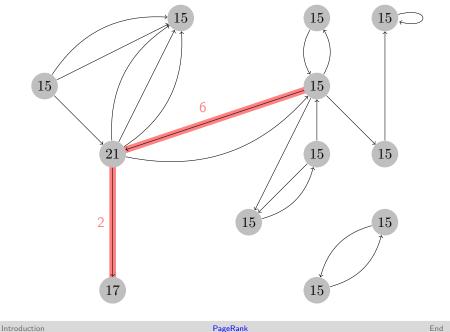
PageRank 00000000000

End 0000000

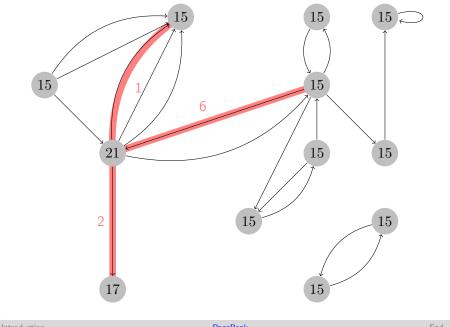


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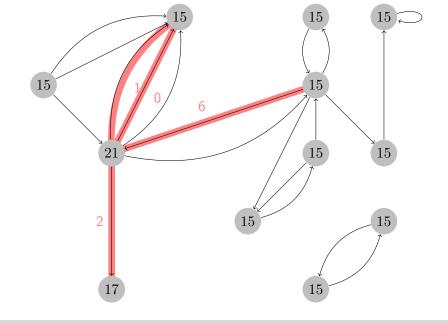


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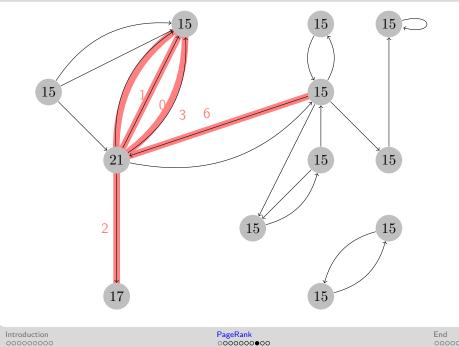
PageRank ○000000●00

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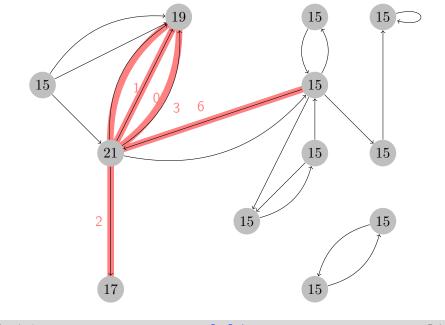
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Mathematics



Let x be a web page. Then

- $lue{L}(x)$ is the set of websites that link to x
- C(y) is the out-degree of page y
- ullet α is probability of random jump

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N is the total number of websites

$$PR(x) := \alpha \left(\frac{1}{N}\right) + (1 - \alpha) \sum_{y \in L(x)} \frac{PR(y)}{C(y)}$$



```
function PAGERANK (Graph web, double q=0.15, int iterations) while iterations>0 do for all page \in web do \qquad > calculate pageRank of page page.pageRank = q for all y \in L(page) do \qquad page.pageRank += \frac{y.pageRank}{C(y)} end for end for iterations -= 1
```

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function PageRank(Graph web, double q=0.15, int iterations) while iterations>0 do for all page \in web do \qquad 
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```
\begin{array}{ll} \textbf{function} \ \mathsf{PAGERANK}\big(\mathsf{Graph} \ web, \ \mathsf{double} \ q = 0.15, \ \mathsf{int} \ iterations\big) \\ \textbf{while} \ iterations > 0 \ \textbf{do} \\ \textbf{for all} \ page \in web \ \textbf{do} \qquad \qquad \rhd \mathsf{calculate} \ \mathsf{pageRank} \ \mathsf{of} \ page \\ page.pageRank = q \\ \textbf{for all} \ y \in L(page) \ \textbf{do} \\ page.pageRank \ += \ \frac{y.pageRank}{C(y)} \\ \textbf{end for} \\ \textbf{end for} \end{array}
```

iterations = 1



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```

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Factors of Influence



- language
- location
- social information: what your friends like

Factors of Influence



- language
- location
- social information: what your friends like

Factors of Influence



- language
- location
- social information: what your friends like

The Filter Bubble



dontbubble.us www.thefilterbubble.com

The Filter Bubble





Introduction

PageRank 000000000

The Filter Bubble





What You've Learned



- web directories
- web crawler
- graph (nodes, eges)
- random walk (ants)
- PageRank
- read pseudocode
- filter bubble

Image Sources



- PageRank by Felipe Micaroni Lalli
- screenshots of www.dmoz.org
- Hyperlink by Bernard Ladenthin
- screenshots of dontbubble.us
- Sergey Brin by enlewof
- Larry Page by aweigend

Thanks for Your Attention!



Days 1 - 10

Teach yourself variables, constants, arrays, strings, expressions, statements, functions....



Davs 11 - 21

Teach yourself program flow. pointers, references, classes, objects, inheritance, polymorphism.



Days 22 - 697

Do a lot of recreational programming. Have fun hacking but remember to learn from your mistakes.



Days 698 - 3648

Interact with other programmers. Work on programming projects together. Learn from them.





Days 3649 - 7781

Teach yourself advanced theoretical physics and formulate a consistent theory of quantum gravity.



Days 7782 - 14611

Teach yourself biochemistry, molecular biology, genetics....



Day 14611

Use knowledge of biology to make an age-reversing potion.



Day 14611

Use knowledge of physics to build flux capacitor and go back in time to day 21.



Day 21

Replace younger self.



As far as I know, this is the easiest way to

"Teach Yourself C++ in 21 Days".